

**AST 300B – Spring 2019**  
**In-class/take-home Problems Due: Jan. 30**

2 pages (see back)

9. Compute the column density and optical depth for the following cases and indicate if the medium is optically thin or optically thick:
- (a) UV photons ( $< 13.6$  eV) elastically scattering off electrons (Thompson scattering) with  $n_e \sim 10^{-2} \text{ cm}^{-3}$  in an HII region with a diameter of 10 pc. Comment on how easy it is for these UV photons to propagate through the HII region.
  - (b) 13.6 eV photons capable of ionizing hydrogen atoms impinging on CNM HI clouds of density  $n_H \sim 1 \text{ cm}^{-3}$  and thickness 1 pc. Comment on how easy it is for these photons to propagate through a CNM HI cloud.

**Table 5.1.** Sample photon interaction cross-sections<sup>a</sup>

Type	Description	Wavelength or energy	Cross-section (cm <sup>2</sup> )
$\sigma_{T^b}$	Thomson scattering	$\ll 0.51 \text{ MeV}$	$6.65 \times 10^{-25}$
$\sigma_{K-N^c}$	Compton scattering	0.51 MeV	$2.86 \times 10^{-25}$
		5.1 MeV	$8.16 \times 10^{-26}$
$\sigma_{R^d}$	Rayleigh scattering (N <sub>2</sub> )	532 nm	$5.10 \times 10^{-27}$
	(CO)	532 nm	$6.19 \times 10^{-27}$
	(CO <sub>2</sub> )	532 nm	$12.4 \times 10^{-27}$
	(CH <sub>4</sub> )	532 nm	$12.47 \times 10^{-27}$
$\sigma_{b-b^e}$	Ly $\alpha$ (natural) <sup>f</sup>	121.567 nm	$7.1 \times 10^{-11}$
	Ly $\alpha$ (10 <sup>4</sup> K) <sup>g</sup>	121.567 nm	$5.0 \times 10^{-14}$
$\sigma_{HI \rightarrow HII^h}$	H ionization	13.6 eV	$6.3 \times 10^{-18}$
$\sigma_{f-f^i}$	free-free absorption	21 cm	$2.8 \times 10^{-27}$

See Irwin for full table footnotes.

10. A spherical optically thick object emits **thermally** at temperature  $T_c$  and is surrounded by an optically thin shell. This shell absorbs/emits **thermally** with temperature  $T_s$ , but only in a narrow spectral line with absorption coefficient plotted below as a function of frequency  $\nu$  (NOTE: that  $\alpha_\nu$  goes to ZERO on each side of the spectral line centered at frequency  $\nu_0$  which means that  $\tau_\nu$  goes to ZERO at those frequencies – i.e. the shell is completely transparent at  $\nu$  away from the spectral line.). You may assume that this spectral line is narrow enough in frequency such that any Planck function is essentially constant in frequency across the line. The total optical depth through the shell at frequency  $\nu_0$  is  $\tau_A$  along ray A and is  $\tau_B$  along ray B. Assume there is no background radiation field outside the central object and shell.

(a) Sketch the spectra (Monochromatic Specific Intensity vs. Frequency) for this spectral line for rays A and B assuming that  $T_s < T_c$ . On the x-axis, label  $\nu_0$  and  $\nu_1$ . On the y-axis, label the continuum level (the intensity level outside the frequency range of the spectral line) and label how high the spectral line peak is above or below the continuum level. **HINT:** Write down a formula for  $\Delta I_\nu$  at  $\nu_0$  where  $\Delta I_\nu$  is the intensity difference between the peak of the spectral line and the continuum level.

(b) Sketch the spectra for this spectral line for rays A and B assuming that  $T_s > T_c$ . Same Hint/axis labelling comments apply.

