

## Table of Ion Critical Densities with e<sup>-</sup>

**Table 18.1** Critical Electron Density  $n_{\text{crit}}(e^-)$  ( $\text{cm}^{-3}$ ) for Selected  $np^2$  and  $np^4$  Ions

Configuration	Ion	$n_{\text{crit}}(e^-)$ at $T = 10^4$ K				
		$^3P_0$	$^3P_1$	$^3P_2$	$^1D_2$	$^1S_0$
$1s^2 2s^2 2p^2$	C I	-	$7.37 \times 10^0$	$1.21 \times 10^1$	-	-
	N II	-	$1.67 \times 10^2$	$2.96 \times 10^2$	$7.68 \times 10^4$	$1.23 \times 10^7$
	O III	-	$1.74 \times 10^3$	$3.79 \times 10^3$	$6.40 \times 10^5$	$2.78 \times 10^7$
	Ne V	-	$3.19 \times 10^5$	$3.48 \times 10^5$	$1.44 \times 10^8$	$9.58 \times 10^8$
$1s^2 2s^2 2p^4$	O I	$3.11 \times 10^3$	$2.87 \times 10^4$	-	$1.62 \times 10^6$	$4.04 \times 10^8$
	Ne III	$3.02 \times 10^4$	$2.76 \times 10^6$	-	$9.47 \times 10^6$	$1.37 \times 10^8$
	Mg V	$4.36 \times 10^6$	$4.75 \times 10^7$	-	$1.07 \times 10^9$	$8.07 \times 10^9$
$1s^2 2s^2 2p^6 3s^2 3p^2$	Si I	-	$7.72 \times 10^2$	$1.92 \times 10^3$	-	-
	S III	-	$4.22 \times 10^3$	$1.31 \times 10^4$	$7.33 \times 10^5$	$1.52 \times 10^7$
	Ar V	-	$1.09 \times 10^7$	$1.16 \times 10^7$	$3.65 \times 10^8$	$2.49 \times 10^8$
$1s^2 2s^2 2p^6 3s^2 3p^4$	S I	$1.04 \times 10^5$	$1.55 \times 10^5$	-	$4.12 \times 10^7$	$1.38 \times 10^9$
	Ar III	$2.49 \times 10^5$	$2.67 \times 10^6$	-	$1.26 \times 10^7$	$4.54 \times 10^8$

**Table 18.2** Critical Electron Density  $n_{\text{crit}}(e^-)$  ( $\text{cm}^{-3}$ ) for Selected  $np^3$  Ions, for  $T = 10^4$  K

Configuration	Ion	$n_{\text{crit}}(e^-)$ at $T = 10^4$ K			
		$^2D_{3/2}^o$	$^2D_{5/2}^o$	$^2P_{1/2}^o$	$^2P_{3/2}^o$
$1s^2 2s^2 2p^3$	N I	$2.18 \times 10^4$	$1.19 \times 10^4$	$7.11 \times 10^7$	$3.15 \times 10^7$
	O II	$4.49 \times 10^3$	$3.31 \times 10^3$	$5.30 \times 10^6$	$1.03 \times 10^7$
	Ne IV	$1.40 \times 10^6$	$4.66 \times 10^5$	$4.17 \times 10^8$	$2.79 \times 10^8$
$1s^2 2s^2 2p^6 3s^2 3p^3$	S II	$1.49 \times 10^4$	$1.57 \times 10^3$	$1.49 \times 10^6$	$1.91 \times 10^6$
	Ar IV	$1.35 \times 10^6$	$1.55 \times 10^4$	$1.06 \times 10^7$	$1.81 \times 10^7$

## Critical Densities for Molecules

Optically thin critical density for collisions with H<sub>2</sub> (Shirley 2015)

Molecule	$j \rightarrow k$	$\nu_{jk}$ (GHz)	$E_j/k$ (K)	$A_{jk}$ (s <sup>-1</sup> )	$n_{\text{ph}}(T_{\text{cmb}})$	$n_{\text{crit}}^{\text{thin, no } b^2}(\text{K}_k)$ cm <sup>-3</sup>			
						10K	20K	50K	100K
HCO <sup>+</sup>	1-0	89.189	4.28	4.3E-5	0.264	6.8E+4	4.5E+4	2.9E+4	2.3E+4
	2-1	178.375	12.84	4.1E-4	0.046	5.6E+5	4.2E+5	2.8E+5	2.2E+5
	3-2	267.558	25.68	1.5E-3	0.009	1.6E+6	1.4E+6	1.0E+6	8.1E+5
H <sup>13</sup> CO <sup>+</sup>	4-3	356.734	42.80	3.6E-3	0.002	3.6E+6	3.2E+6	2.5E+6	2.0E+6
	1-0	86.754	4.16	3.9E-5	0.279	6.2E+4	4.1E+4	2.7E+4	2.0E+4
	2-1	173.507	12.49	3.7E-4	0.050	5.1E+5	3.8E+5	2.6E+5	2.0E+5
N <sub>2</sub> H <sup>+</sup>	3-2	260.255	24.98	1.3E-3	0.011	1.5E+6	1.3E+6	9.5E+5	7.3E+5
	4-3	346.998	41.63	3.3E-3	0.002	3.4E+6	2.9E+6	2.3E+6	1.8E+6
	1-0	93.174	4.47	3.6E-5	0.242	6.1E+4	4.1E+4	2.6E+4	2.0E+4
HCN	2-1	186.345	13.41	3.5E-4	0.040	5.0E+5	3.7E+5	2.6E+5	1.9E+5
	3-2	279.512	26.83	1.3E-3	0.007	1.4E+6	1.2E+6	9.2E+5	7.1E+5
	4-3	372.673	44.71	3.1E-3	0.001	3.2E+6	2.8E+6	2.2E+6	1.7E+6
H <sup>13</sup> CN	1-0	88.632	4.25	2.4E-5	0.268	4.7E+5	3.0E+5	1.7E+5	1.1E+5
	2-1	177.261	12.76	2.3E-4	0.047	4.1E+6	2.8E+6	1.6E+6	1.1E+6
	3-2	265.886	25.52	8.4E-4	0.010	1.4E+7	1.0E+7	5.7E+6	3.8E+6
HNC	4-3	354.505	42.53	2.1E-3	0.002	3.0E+7	2.3E+7	1.4E+7	9.1E+6
	1-0	86.340	4.14	2.2E-5	0.282	5.3E+5	2.5E+5	1.3E+5	9.7E+4
	2-1	172.678	12.43	2.1E-4	0.051	3.4E+6	2.2E+6	1.2E+6	9.1E+5
CN	3-2	259.012	24.86	7.7E-4	0.011	8.8E+6	6.6E+6	4.1E+6	3.3E+6
	4-3	345.340	41.43	1.9E-3	0.002	1.9E+7	1.5E+7	9.7E+6	7.7E+6
	1-0	90.664	4.35	2.7E-5	0.256	1.4E+5	1.1E+5	8.4E+4	7.0E+4
CS	2-1	181.325	13.05	2.6E-4	0.043	1.3E+6	1.0E+6	8.2E+5	6.8E+5
	3-2	271.981	26.11	9.3E-4	0.009	5.1E+6	4.0E+6	3.1E+6	2.5E+6
	4-3	362.630	43.51	2.3E-3	0.002	1.3E+7	1.0E+7	7.8E+6	6.2E+6
p-NH <sub>3</sub> <sup>c</sup>	$3_{3/2} - 2_{3/2}$	113.495	5.45	1.2E-5	0.158	4.1E+5	2.4E+5	1.1E+5	6.4E+4
	$2_{5/2} - 1_{3/2}$	226.876	16.34	1.1E-4	0.019	3.2E+6	2.2E+6	1.1E+6	6.4E+5
	$3_{7/2} - 2_{5/2}$	340.249	32.66	4.1E-4	0.003	8.3E+6	6.5E+6	3.5E+6	2.1E+6
o-NH <sub>3</sub> <sup>c</sup>	1-0	48.991	2.40	1.7E-6	0.734	1.5E+4	1.1E+4	7.8E+3	5.7E+3
	2-1	97.981	7.10	1.7E-5	0.218	1.3E+5	1.0E+5	7.4E+4	5.5E+4
	3-2	146.969	14.10	6.1E-5	0.082	4.4E+5	3.6E+5	2.6E+5	2.0E+5
$2_1^+ - 1_1^-$	4-3	195.954	23.50	1.5E-4	0.033	1.0E+6	8.6E+5	6.4E+5	4.8E+5
	5-4	244.936	35.30	3.0E-4	0.014	2.0E+6	1.7E+6	1.3E+6	9.5E+5
	6-5	293.912	49.40	5.2E-4	0.006	3.4E+6	2.9E+6	2.2E+6	1.6E+6
$2_2^- - 1_2^+$	7-6	342.883	65.80	8.4E-4	0.002	5.0E+6	4.4E+6	3.4E+6	2.6E+6
	(1,1)	23.694	1.14	1.7E-7	1.940	2.0E+3	1.8E+3	1.2E+3	8.7E+2
	(2,2)	23.723	42.32	2.3E-7	1.937	1.6E+3	1.5E+3	1.4E+3	1.1E+3
$1_0 - 0_0$	$2_1^+ - 1_1^-$	1168.452	57.21	1.2E-2	0.000	1.2E+8	1.1E+8	9.0E+7	6.7E+7
	$2_2^- - 1_2^+$	1215.245	58.32	1.4E-2	0.000	1.4E+8	1.2E+8	1.0E+8	7.5E+7
	(3,3)	23.870	123.54	2.6E-7	1.923	1.5E+3	1.5E+3	1.4E+3	1.2E+3
$1_0 - 0_0$	572.498	27.48	1.6E-3	0.000	4.0E+7	3.1E+7	1.7E+7	9.9E+6	